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Occupational Choice, Human Capital, and Financial Constraints*

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Abstract

We study the aggregate productivity effects of firm-level financial frictions. Credit constraints affect not only production decisions, but also household-level schooling decisions. In turn, entrepreneurial schooling decisions impact firm-level productivities, whose cross-sectional distribution becomes endogenous. In anticipation of future constraints, entrepreneurs under-invest in schooling early in life. Frictions lower aggregate productivity because talent is misallocated across occupations, and capital misallocated across firms. Firm-level productivities are also lower due to schooling distortions. These effects combined account for between 36 and 68 percent of the U.S.-India aggregate productivity difference. Schooling distortions are the major source of aggregate productivity differences.

Keywords: Aggregate Productivity, Financial Frictions, Entrepreneurship, Human Capital, Misallocation.

JEL Codes: E24, I25, J24, O11, O15, O16, O47.

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1 Introduction

Total Factor Productivity (TFP) is the single most important factor accounting for the large cross-country income differences we see in the data (Klenow and Rodríguez-Clare, 1997; Hall and Jones, 1999; Caselli, 2005; Hsieh and Klenow, 2010). We evaluate the quantitative significance of financial frictions as a source of TFP differences. Entrepreneurs face a standard collateral constraint when raising business capital. Our main contribution is to consider also the role of entrepreneurial schooling decisions, and how they interact with financial frictions.

We view entrepreneurial human capital as a main determinant of firm-level productivity. Consistent with the evidence we provide, skills vary widely among entrepreneurs, with the more educated ones being better managers, more aware and skilled at implementing better management practices (Bloom and Reenen, 2007), and therefore operate more productive businesses. In this setting, future entrepreneurs under-invest in schooling in anticipation of credit constraints. They do so because investing in schooling is not very productive in small-sized firms, and also because the opportunity cost of schooling investments is high when resources could be used instead to build up collateral. In other words, entrepreneurs don't invest much in education since they realize they will be running a small family business; they prefer instead to work hard in order to save more. Further, schooling investments get misallocated. That is, those entrepreneurs with the best productivity potential are the ones who feel compelled to reduce schooling investments the most. We find that these two effects, schooling under-investment and schooling misallocation, play a very important quantitative role in accounting for the U.S.-India TFP difference. They jointly contribute to most of the model-generated variation.

Our model bridges two literatures/frameworks. One is a model of entrepreneurship with credit constraints, along the lines of Buera and Shin (2013) and Midrigan

and Xu (2014), among others.¹ The other is a model of human capital accumulation along the lines of Erosa, Koreshkova and Restuccia (2010) and Manuelli and Seshadri (2014).

Like in the existing literature on entrepreneurship with credit constraints, financial frictions generate misallocation of talent across occupations. Poor individuals talented at entrepreneurship choose to become workers, since their firms would operate at an inefficiently small scale. Other individuals, not so talented at managing and operating a production technology, find it advantageous to do so if sufficiently wealthy. Further, capital gets misallocated across those individuals that do decide to become entrepreneurs. This is because with credit constraints firm size depends on entrepreneurial wealth, not just firm-level productivity. On top of these well-understood effects of credit constraints, our framework generates additional ones, stemming from adjustments in entrepreneurial schooling choices and in the distribution of firm-level productivities. A key feature of our setup is precisely that the distribution of firm-level productivities becomes endogenous, determined by entrepreneurial-level schooling decisions.

We quantify the role of these different effects of credit frictions on TFP. In line with the previous literature, we first calibrate our model to the U.S. and consider a scenario where the only fundamental difference between the U.S. and India is the overall degree of financial frictions. In this case, our model accounts for 36 percent of the U.S.-India TFP difference. A second calibration also lets the average productivity of the human capital accumulation technology vary across the U.S. and India in order to match the average years of schooling differences across these two countries. This results in a significant amplification of the effect

¹Other references include Castro, Clementi and MacDonald (2004, 2009), Jeong and Townsend (2007), Erosa and Hidalgo-Cabrillana (2008), Amaral and Quintin (2010), Buera, Kaboski and Shin (2011), Greenwood, Sanchez and Wang (2013), Moll (2014), Cole, Greenwood and Sanchez (2016), and Moll, Townsend and Zhorin (2017).

of frictions, namely entrepreneurial schooling under-investment and misallocation, and the model accounts for 68 percent of the observed TFP difference.

Our modelling of schooling decisions follows [Erosa, Koreshkova and Restuccia \(2010\)](#) and [Manuelli and Seshadri \(2014\)](#). These papers emphasize the role of cross-country TFP differences in generating variation in human capital outcomes ([Manuelli and Seshadri, 2014](#), also consider cross-country variation in relative prices of capital and demographics). Our model shares the feature that, in addition to time, expenditure in goods (or resource-based education quality) is also a key input into the human capital accumulation process. As in these papers, the education quality margin in our model leads workers to invest less in education in countries with lower wages (due to tighter credit frictions in our case). In our paper credit frictions also discourage schooling investments among entrepreneurs, by reducing the marginal return to those investments. The latter mechanism is independent from the presence of an education quality margin in the human capital accumulation process.² More generally, rather than studying the implications of a given exogenous degree of cross-country TFP differences for schooling outcomes, our key contribution is to highlight the role of entrepreneurial schooling decisions in shaping TFP, when entrepreneurs are subject to financial frictions.

[Bhattacharya, Guner and Ventura \(2013\)](#) also consider entrepreneurial investment in managerial skills, in a setting with exogenously given distortions in firm size. Larger distortions discourage skill investments by managers. As in their paper, the distribution of firm-level productivities in our model arises endogenously from

²An extensive literature deals with educational decisions under credit constraints. An early example is [Galor and Zeira \(1993\)](#), and more recent developments are in [Lochner and Monge-Naranjo \(2011\)](#) and [Córdoba and Ripoll \(2013\)](#). As in these papers, our credit constraints also act as a direct mechanism lowering education, namely among poorer individuals. The central role of credit constraints in our model, however, is in affecting entrepreneurial, not worker, schooling decisions. In other words, rather than increasing current schooling costs for poor workers, credit constraints in our model act primarily on lowering the net future benefit of schooling for poor entrepreneurs.

entrepreneurial investments in human capital. In contrast to their framework, firm size distortions are endogenous here, and depend on the wealth distribution. In our model, constrained entrepreneurs under-invest in schooling partially in order to self-finance. This mitigates physical capital misallocation across firms, a mechanism also emphasized by [Midrigan and Xu \(2014\)](#). Closer to our paper, [Mestieri, Schauer and Townsend \(2017\)](#) focus on distortions arising from the presence of financial frictions. Their main goal, however, is contrasting the model’s implications for individual-level behavior with Mexican data, namely life-cycle dynamics of entrepreneurship, and how schooling and occupational decisions depend upon household characteristics.

Finally, our paper is also related to the resource misallocation literature, namely [Restuccia and Rogerson \(2008\)](#), [Hsieh and Klenow \(2009\)](#), and [Bartelsman, Haltiwanger and Scarpetta \(2013\)](#). These authors examine the aggregate productivity consequences of misallocation generated by firm-specific taxes and subsidies. These taxes and subsidies are effectively stand-in, generic distortions, meant to capture deeper allocative problems. Our model concentrates on one such allocative problem: malfunctioning credit markets. We provide an explicit mapping between fundamental distortions coming out of our model, which have a structural interpretation, and the stand-in taxes and subsidies that are typically considered in this literature. In the process, we extend [Hsieh and Klenow’s \(2009\)](#) framework for measuring the extent of resource misallocation. In our case, in addition to distortions to cross-firm input allocation, there are also distortions impacting physical productivity relative to the frictionless benchmark. The latter are induced by talent misallocation and by distortions to entrepreneurial schooling investments, and play the largest quantitative role.

The paper is organized as follows. Section [2](#) describes the model. Section [3](#) analyzes the individual decisions and the aggregate productivity effects of distortions.

Section 4 presents evidence on the significance of schooling for entrepreneurship. Section 5 describes the calibration procedure. Section 6 presents the quantitative results, and Section 7 concludes. The Appendices contain detailed information about the formal definition of equilibrium, some of the analytical properties of the model, the mapping between model and data, and the numerical procedure.

2 Model

2.1 The Environment

Consider an economy with measure one of altruistic dynasties. Each individual lives for 2 periods, childhood and adulthood. The household, composed of a child and an adult parent, is the decision unit (unitary household model). We call childhood the period when schooling and investment decisions are made, and adulthood the period when the individual's main economic activity is carried out. Households value stochastic aggregate household consumption streams according to

$$\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t u(c_t), \quad (1)$$

where $\beta \in (0, 1)$ is the time and generation discount factor. The period utility function u is of class C^2 , strictly increasing, strictly concave, and satisfies the usual Inada conditions.

In anticipation of our recursive formulation, we use primes to denote variables pertaining to the next generation, whereas those without primes refer to the current one. The household starts the period with wealth ω , and a draw of the child's abilities, current learning ability $z > 0$, and future entrepreneurial ability $x > 0$. The inter-generational ability transmission is governed by a first-order Markov chain

with transition probabilities $\pi(z', x' | z, x)$.

Given the current state (ω, z, x) , the household makes four decisions. First, it decides today's investment in the child's education, by choosing schooling time s and schooling expenditures e to produce human capital according to

$$h = z \left(s^\eta e^{1-\eta} \right)^\xi, \quad (2)$$

with $\eta \in [0, 1]$ and $\xi \in [0, 1]$.³ We follow [Erosa, Koreshkova and Restuccia \(2010\)](#) and [Manuelli and Seshadri \(2014\)](#) in considering expenditures as an input to human capital accumulation in addition to student time. This allows a worker's schooling time to increase with wages. With the presence of expenditures, higher wages increase the marginal gain from schooling investments by more than the marginal cost, since the price of the goods input is invariant to the wage.⁴

Second, the household decides today's saving for next period, by purchasing bonds in net amount q at unit price $1/(1+r)$. We assume ability shocks are uninsurable.⁵ Third, it decides the child's occupation for next period, whether to become an entrepreneur or a worker. Workers supply their human capital at the going wage rate. Entrepreneurs manage their own firms and are the residual claimants of profits. Fourth, if the decision is to become an entrepreneur next period then the household also needs to raise capital, possibly with external funds, and hire labor in

³A more general formulation would be $h = z \left(s^\eta e^{1-\eta} \right)^\xi \bar{h}_0^\xi + (1 - \delta_h) \bar{h}_0$, where \bar{h}_0 is the child's initial human capital. We assume $\delta_h = 1$, similarly to [Erosa, Koreshkova and Restuccia \(2010\)](#). The component \bar{h}_0^ξ is captured by mean learning ability in our specification. Intergenerational transmission of human capital is therefore governed by the persistence in learning ability.

⁴As in [Erosa, Koreshkova and Restuccia \(2010\)](#), this also relies on the presence of tuition costs, which we also model. Tuition costs prevent the marginal gains and costs from an additional year of schooling to both vary proportionally with the current level of human capital, allowing schooling years to vary with both learning ability z and, via school quality adjustments, wages.

⁵Given our assumption on the resolution of uncertainty, saving is contingent upon the child's abilities, namely next period's entrepreneurial ability. We abstract from precautionary saving behavior associated with entrepreneurial ability risk in order to streamline the analysis. This allows us to characterize the household investment decisions via simple non-arbitrage conditions.

order to run the firm.

All production is carried out by entrepreneurs according to

$$y = xh^{1-\gamma} \left(k^\alpha l^{1-\alpha} \right)^\gamma, \quad (3)$$

with $\alpha, \gamma \in (0, 1)$, where k and l denote physical capital and labor inputs. It is convenient to define entrepreneurial, or firm-level productivity as $a^{1-\gamma} \equiv xh^{1-\gamma}$, where x is determined by luck and h is the entrepreneur's human capital level. Physical capital depreciates at rate $\delta \in (0, 1)$.

2.2 Household's Problem

We focus on stationary equilibria, in which prices and the cross-sectional distribution over individual states are time-invariant. Denote by w the wage rate (unit price of human capital) and by r the real interest rate. We begin by formulating the household's problem conditional on the child's occupational choice. Notice that, since all uncertainty is resolved at the start of an individual's life, the occupational choice can be made right then.

Conditional on the child becoming a worker next period, the worker-household's (worker, for short) problem can be written recursively as:

$$v^w(\omega, z, x) = \max_{c, e, s, q} \left\{ u(c) + \beta \sum_{z', x'} \pi(z', x' | z, x) v(\omega', z', x') \right\} \quad (\text{Pw})$$

subject to (2) and

$$c + ws\bar{l} + e + \frac{1}{1+r}q = w\psi h(1-s) + \omega \quad (4)$$

$$s \leq \bar{s} \quad (5)$$

$$q \geq -\lambda\phi \max\{\omega, 0\} \quad (6)$$

$$\omega' \equiv wh + q. \quad (7)$$

Equation (4) is the budget constraint. The term $ws\bar{l} + e$ is the direct cost of investing in the child's education, tuition fees $ws\bar{l}$ (\bar{l} is the total teacher input per unit of student time, a parameter) plus expenditures in education quality e . Teacher's effective time is not an input into human capital production, only student time is. Expenditures in goods capture direct costs such as books and computers. On the right-hand-side, $w\psi h(1-s)$ is the child's labor earnings, where $\psi \in (0, 1)$ captures increasing labor earnings over an individual's lifetime due to experience.

Equation (5) is the child's time constraint (our assumptions on preferences and human capital technology allow us to ignore the non-negativity constraints on consumption, time, and schooling expenditures). We impose an upper bound $\bar{s} \leq 1$ for quantitative purposes, since individuals do not normally spend their entire early life studying.

Households are subject to an inter-period *household credit constraint* given by (6). They can only contract debt up to a multiple $\lambda\phi \geq 0$ of their wealth.⁶ When $\phi = 0$ no borrowing is allowed, and investment must be funded out of the household's

⁶This constraint can be motivated by a simple static limited enforcement problem. Suppose a household decides whether to default on the loan repayment $-q$. The only penalty is that financial intermediaries may seize a fraction $\nu \in [0, 1]$ of initial wealth $\omega > 0$, net of q . Intermediaries then require that the gain from defaulting does not exceed the cost, that is $-(1-\nu)q \leq \nu\omega$. This yields (6) with $\phi\lambda \equiv \nu/(1-\nu) \geq 0$. The main advantage from using this simple specification is tractability. It shares with self-enforcing limits based on dynamic incentives (Kehoe and Levine, 1993) the key feature that richer households are able to borrow more.

wealth; when $\phi = \infty$ (provided $\lambda > 0$, which we assume) access to household credit is unconstrained. Equation (7) defines the initial wealth of the next household in the dynastic line, conditional on the fact that next period's parent will be a worker.

Similarly, conditional on the child becoming an entrepreneur next period, the entrepreneur-household's (entrepreneur, for short) problem reads:

$$v^e(\omega, z, x) = \max_{c, e, s, q} \left\{ u(c) + \beta \sum_{z', x'} \pi(z', x' | z, x) v(\omega', z', x') \right\} \quad (\text{Pe})$$

subject to (2)–(6) and a new definition of household's wealth based upon entrepreneurial profits

$$\omega' \equiv \Pi(q, h, x) + q, \quad (8)$$

where

$$\Pi(q, h, x) = \max_{k, l \geq 0} \left\{ a^{1-\gamma} \left(k^\alpha l^{1-\alpha} \right)^\gamma - (r + \delta)k - wl \right\} \quad (\text{Pf})$$

subject to

$$k \leq \lambda \frac{q}{1+r}, \quad (9)$$

with $\lambda \geq 1$. Entrepreneurs hire capital and labor to maximize profits, subject to an intra-period *capital constraint*. The maximum level of capital an entrepreneur can employ in production is given by a multiple λ of the household's second period assets, which acts as collateral.⁷ When $\lambda = 1$ no external funding is allowed, and capital is solely determined by internal funds. When $\lambda = \infty$ financial markets work

⁷We assume future profits are not pledgable as collateral. Constraint (9) therefore implies that households that borrow today will not be able to run a firm tomorrow. As a result, only children from sufficiently wealthy backgrounds can aspire to become entrepreneurs. Similarly to (6), the constraint (9) may be motivated by a simple static limited enforcement problem. As in Buera and Shin (2013), suppose households borrow k from financial intermediaries against collateral $\frac{q}{1+r}$, and then have a decision whether to default. The only penalty is that intermediaries may seize the entire collateral, plus a fraction of κ of k . No default requires $(1-\kappa)k \leq \frac{q}{1+r}$, which yields (9) with $\lambda \equiv 1/(1-\kappa) \geq 1$. Related work using identical collateral constraints include Evans and Jovanovic (1989), Moll (2014) and Moll, Townsend and Zhorin (2017).

perfectly, and capital is not constrained by wealth.

Financial frictions affect the model via (6) and (9). The parameter λ governs the overall extent of financial frictions in the economy, whereas ϕ controls the household credit constraint. We choose this formulation to reflect the possibility that seizing wealth upon default, for example, might be easier for one type of credit compared to the other. In our quantitative analysis we let λ vary across countries while fixing ϕ .

The household's occupational choice for the child next period is then

$$v(\omega, z, x) = \max \{v^w(\omega, z, x), v^e(\omega, z, x)\}. \quad (10)$$

Appendix A has the formal definition of a stationary recursive competitive equilibrium.

3 Analysis

Our first task is to obtain expressions illustrating how financial frictions affect investment decisions in our model. We show in particular how the capital constraint that entrepreneurs will face later in life while active in production distort schooling investments earlier in life. We then use the expressions encapsulating distortions to derive the aggregate TFP implications.

3.1 Production

Conditional on their human capital, entrepreneurs hire labor and capital to maximize profits. The presence of the capital constraint implies the profit function:

$$\Pi(q, h, x) = \begin{cases} \Pi^*(h, x) & \text{if } q \geq q^*(h, x) \text{ (unconstrained)} \\ \Pi^c(q, h, x) & \text{else (constrained),} \end{cases}$$

where $q^*(h, x)$ is a threshold level of assets beyond which the capital constraint does not bind. Appendix B provides the expressions for threshold assets, as well as for the constrained and unconstrained profit functions. The constrained profit function is increasing in accumulated assets since a higher q allows the entrepreneur to raise more capital and increase the scale of the firm closer to its optimal level.

3.2 Schooling/Saving Decisions

Individuals can invest either through bonds, or by spending time and resources on schooling. Our timing assumption allows us to characterize these different investment opportunities in terms of simple non-arbitrage equations that transpire from the first-order optimality conditions for problems (Pw) and (Pe) with respect to s , e , and q (Appendix C). From the optimality conditions, schooling time is an implicit function $s(e)$ of schooling expenditures,

$$w(\bar{l} + \psi h) = \frac{\eta}{1 - \eta} \frac{e}{s},$$

where s is strictly increasing in e , since both inputs are complements in human capital production. Replacing in (2) yields human capital $h(e)$.

The optimality conditions then deliver our key non-arbitrage condition equating

the returns to saving and human capital accumulation:

$$(1 - \eta) \xi \frac{h(e)}{e} \omega'_2(q, h(e), x) = (1 + r) p_e(e) \omega'_1(q, h(e), x), \quad (11)$$

where ω'_1 and ω'_2 are the partial derivatives of future wealth with respect to the first and the second arguments, capturing the returns to saving and to human capital, respectively. For convenience we denote the shadow unit price of schooling expenditures by

$$p_e = p_e(e) \equiv 1 - w\psi(1 - s(e))(1 - \eta) \xi \frac{h(e)}{e}, \quad (12)$$

which equals the unit of foregone consumption net of the marginal increase in first-period earnings. Specializing (11) for each occupation allows us to characterize the optimal schooling decisions for workers and entrepreneurs.⁸

3.2.1 Worker-Household

For workers we have

$$\omega'_1(q, h, x) = 1 \text{ and } \omega'_2(q, h, x) = w. \quad (13)$$

Since wages are linear in worker's human capital, returns to human capital accumulation are constant. From (11), an interior optimum for schooling expenditures solves:

$$\frac{w}{1 + r} (1 - \eta) \xi \frac{h}{e} = p_e. \quad (14)$$

The left-hand-side is the discounted future benefit of investing an extra unit of the final good on education, which is the wage rate times the marginal increase in

⁸An optimal solution always exists since $(1 - \eta)\xi < 1$.

human capital. The right-hand-side is the marginal cost, which is the unit of the good invested less the marginal increase in labor earnings enjoyed in the current period.

When the borrowing constraint binds ($q = -\lambda\phi\omega$), optimal expenditures cannot be pinned-down by (11), and are instead the solution to a dynamic optimization problem. Schooling investments are then a function not just of learning ability, but also of current wealth ω .

3.2.2 Entrepreneur-Household

The capital constraint (9), together with the condition that $k \geq 0$, implies that entrepreneurs will always have $q > 0$ and therefore the constraint on household credit will never bind. We have:

$$\omega'_1(q, h, x) = \begin{cases} 1 + \frac{\partial \Pi^c}{\partial q}(q, h, x) & \text{if constrained} \\ 1 & \text{if unconstrained,} \end{cases} \quad (15)$$

and

$$\omega'_2(q, h, x) = \begin{cases} B(q) \frac{1-\gamma}{\alpha\gamma+1-\gamma} a^{\frac{1-\gamma}{\alpha\gamma+1-\gamma}} h^{-1} & \text{if constrained,} \\ Ax^{\frac{1}{1-\gamma}} & \text{if unconstrained,} \end{cases} \quad (16)$$

where the expressions for $B(q)$ and A , which depend on parameters and equilibrium prices, are given in Appendix B. From here we can deduce how the marginal returns to physical and human capital accumulation vary with the entrepreneur's saving q .

Proposition 1. *Given h , capital-constrained entrepreneurs (with $q < q^*(x, h)$) face a higher marginal return to physical capital accumulation and a lower marginal return to human capital accumulation than unconstrained entrepreneurs (with $q \geq q^*(x, h)$).*

Proof. The first part follows from (15), the fact that $\frac{\partial \Pi^c(q, h, x)}{\partial q}$ is decreasing in q , and that $\frac{\partial \Pi^c}{\partial q}(q^*(h, x), h, x) = 0$. The second part follows from (16), the fact that $B(q)$ is increasing in q , and that $B(q^*(h, x)) \frac{1-\gamma}{\alpha\gamma+1-\gamma} a^{\frac{1-\gamma}{\alpha\gamma+1-\gamma}} h^{-1} = Ax^{\frac{1}{1-\gamma}}$. \square

The first part of Proposition 1 comes from the fact that, for capital-constrained entrepreneurs, saving relaxes the capital constraint and allows them to expand their firms closer to the optimal unconstrained scale. The second part holds because human and physical capital are complements in production. Capital-constrained entrepreneurs employ less physical capital, making human capital less productive.

Proposition 1 establishes the central mechanism in our paper, that the anticipation of the capital constraint distorts saving and schooling decisions of entrepreneurs early in life. Constrained households therefore have an incentive to save more and invest less in education compared to unconstrained ones.

Substituting ω'_1 and ω'_2 for unconstrained entrepreneurs into (11) yields their condition for optimal schooling expenditures:

$$\frac{A}{1+r} (1-\eta) \xi \frac{a}{e} = p_e.$$

This condition is analogous to (14), with the left-hand side representing now the discounted marginal increase in future profits from investing an additional unit of the final good on schooling.

For constrained entrepreneurs we obtain:

$$\frac{B(q)}{1+r} (1-\eta) \xi \frac{1-\gamma}{\alpha\gamma+1-\gamma} a^{\frac{1-\gamma}{\alpha\gamma+1-\gamma}} \frac{1}{e} = p_e \left(1 + \frac{\partial \Pi^c}{\partial q}(q, h, x) \right).$$

Compared to the unconstrained case, the marginal gain from investing in education is lower, and decreasing returns set in faster (Proposition 1). The marginal cost is also higher, since investing in education sacrifices wealth accumulation, which lowers

firm capital and hence profits. Optimal spending in education therefore depends on household wealth, via saving q . Higher wealth helps relax the capital constraint, and reduces investment and schooling distortions.

3.3 Input Misallocation and Firm–Level Productivity Effects

We now characterize the input misallocation and the firm–level productivity effects stemming from financial frictions, namely the capital constraint. We borrow from the existing literature on input misallocation, namely [Hsieh and Klenow \(2009\)](#), to map these effects into aggregate TFP.

Our strategy follows in two steps. First, we show that the generic production distortions considered by [Hsieh and Klenow \(2009\)](#) have a structural interpretation in terms of our model. Second, we generalize their framework in the sense that model-based TFP differences are decomposed (subject to a distributional assumption on distortions and firm-level productivities) into not just an input misallocation effect, but also firm–level productivity effects. The latter features the distortions introduced via entrepreneurial investments in human capital. The main advantage of pursuing this approach is that we are able to obtain a decomposition of the aggregate TFP effects into easily interpretable components.

3.3.1 Basic Model Wedges

The capital constraint introduces what amounts to individual-level wedges on the optimal conditions for saving and human capital expenditures. These distortions, which have a structural interpretation, are *basic model wedges*. We first define them, and then show how they map into *proxy*, or stand-in misallocation *wedges*. The latter are like the generic wedges featured in much of the misallocation literature, for example [Restuccia and Rogerson \(2008\)](#), [Hsieh and Klenow \(2009\)](#) and [Bartelsman,](#)

Haltiwanger and Scarpetta (2013), among many others. Since our focus is on production distortions, we shall concentrate on entrepreneurs.

We are able to summarize the effect of the capital constraint on an entrepreneur's optimality conditions (Appendix C) via two basic individual-specific wedges which we label τ_q^e and τ_h^e . That is, we can rewrite these conditions simply as

$$u'(c) = \beta(1+r) \left(1 + \tau_q^e\right) \sum_{z',x'} \pi(z',x'|z,x) v_1(\omega',z',x'), \quad (17)$$

$$p_e u'(c) = \beta(1-\eta) \xi(1 - \tau_h^e) A \frac{a}{e} \sum_{z',x'} \pi(z',x'|z,x) v_1(\omega',z',x'). \quad (18)$$

As long as basic wedges subsume the distortions affecting the marginal value of saving and human capital, (15) and (16), then these simple optimality conditions deliver the solution to the original problem. The appropriate wedges, which are functions of the current individual state, are defined by comparing the optimality conditions for constrained and unconstrained entrepreneurs, yielding:

$$\tau_q^e = \begin{cases} \partial \Pi^c(q, h, x) / \partial q & \text{if constrained,} \\ 0 & \text{if unconstrained,} \end{cases}$$

$$\tau_h^e = \begin{cases} 1 - \frac{B(q)}{A} \frac{1-\gamma}{\alpha\gamma+1-\gamma} a^{-\frac{\alpha\gamma}{\alpha\gamma+1-\gamma}} & \text{if constrained,} \\ 0 & \text{if unconstrained,} \end{cases}$$

The wedge $\tau_q^e \geq 0$ acts like a subsidy to saving, capturing the fact that whenever the capital constraint binds, an increase in saving today relaxes it and increases profits tomorrow. That is, for constrained entrepreneurs, $\frac{\partial \Pi^c}{\partial q}(q, h, x) > 0$.

The wedge $\tau_h^e \in [0, 1]$ acts like a tax on the returns to schooling, capturing the fact that human capital is less productive for constrained entrepreneurs. This is because physical capital is lower, and human capital is complementary to physical capital.

3.3.2 Proxy Production Wedges

We now recast the firm's problem as in [Hsieh and Klenow \(2009\)](#). We call it the proxy firm problem:

$$\Pi = \max_{k, l \geq 0} \left\{ (1 - \tau_a) p (a^*)^{1-\gamma} \left(k^\alpha l^{1-\alpha} \right)^\gamma - (1 + \tau_k) (r + \delta) k - wl \right\}, \quad (\text{Pf'})$$

where we define potential productivity as $(a^*)^{1-\gamma} \equiv x (h^*)^{1-\gamma}$, with h^* being the human capital level that would emerge if the capital constraint did not bind, and p the output price, which may be normalized to 1 in our setup.

We label τ_a and τ_k individual-level *proxy wedges*, in the sense that they are generic wedges standing-in for the fundamental distortions affecting the economy. τ_a captures distortions along the potential revenue (i.e. based on potential productivity) vs cost margin, whereas τ_k captures distortions along the capital vs labor input cost margin. Our task is now to infer proxy wedges from basic wedges, and uncover the unique mapping between the two. The proxy firm problem (Pf') yields the same solution as the original one (Pf) when

$$1 - \tau_a = \left(\frac{h}{h^*} \right)^{1-\gamma}$$

$$1 + \tau_k = 1 + \frac{\zeta}{r + \delta},$$

where ζ is the multiplier on the capital constraint.

Applying the Envelope theorem and using the definition of τ_q^e :

$$1 + \tau_k = 1 + \frac{\tau_q^e (1 + r)}{\lambda (r + \delta)}.$$

Under certain parametric restrictions, τ_a is also an explicit function of basic wedges. This is the case when $\psi = 0$, so that $p_e = 1$. Further assuming that the

time constraint is slack, optimal schooling time s is proportional to expenditures e . We then obtain

$$1 - \tau_a = \left(\frac{1 - \tau_h^e}{1 + \tau_q^e} \right)^{\frac{(1-\gamma)\xi}{1-\xi}}.$$

The last two expressions allow us to structurally interpret the two proxy wedges in terms of our financial frictions model. First, $\tau_k \geq 0$ amounts to a tax on capital. The reason is that the capital constraint increases the shadow rental price of capital. Second, $\tau_a \in [0, 1]$ amounts to a reduction in a firm's physical output. The reason is that the capital constraint decreases actual firm-level productivity $a^{1-\gamma}$ below potential, by discouraging entrepreneurial schooling investments. The total disincentive to investing in human capital is captured by the composite distortion $(1 - \tau_h^e)/(1 + \tau_q^e)$. It amounts to a positive tax since (i) capital-constrained entrepreneurs run smaller firms, reducing the returns to investing in human capital, and (ii) for these households, accumulating wealth relaxes the capital constraint, and therefore commands a higher return compared to investing in human capital.⁹

We can get further insight when $\bar{l} = 0$ (and $\psi > 0$), assuming again a slack time constraint. We obtain in this case

$$1 - \tau_a = \left(\frac{1 - \tau_h^e}{1 + \tau_q^e} \right)^{\frac{1-(1-\gamma-\eta)\xi}{\xi(1-\gamma)^2}} \left(\frac{p_e^*}{p_e} \right)^{\frac{1-(1-\gamma-\eta)\xi}{\xi(1-\gamma)^2}}, \quad (19)$$

where p_e^* is defined as the shadow unit price of schooling expenditures ignoring credit constraints. Although a closed form is not available (p_e is itself a function of basic distortions), this formulation helps illustrate the role of schooling expenditure

⁹Why do financial frictions generate a disincentive to human capital accumulation ($\tau_a > 0$)? Why don't frictions encourage entrepreneurs to invest more in schooling, and therefore generate higher first-period labor earnings per working time? Both are in fact feasible options for entrepreneurs in our model to generate higher savings and more self-financing. However, frictions increase the shadow interest rate ($\tau_q^e > 0$), and the non-arbitrage condition (11) needs to hold. Since investment in schooling exhibits decreasing marginal returns, this can only be the case if schooling declines.

prices in amplifying the effect of basic distortions on the composite distortion τ_a , especially for individuals with low learning ability z (or in a country with low average learning efficiency \bar{z} , as we will explore later). Recall from (12) that p_e equals one unit of the final good net of the increase in first-period earnings afforded by the additional human capital. Individuals with lower first-period earnings (lower z) tend to have higher p_e , and especially higher p_e^* . A higher p_e^*/p_e means schooling investments are more expensive for them - individuals who cannot generate sufficient resources when young, cannot also build up sufficient collateral for when they become entrepreneurs. This amplification mechanism is present in our general formulation, and will play a key role when comparing economies with different \bar{z} .

The production technology underlying the stand-in problem (Pf) is $y \equiv (1 - \tau_a) (a^*)^{1-\gamma} (k^\alpha l^{1-\alpha})^\gamma$. We follow Foster, Haltiwanger and Syverson (2008) and Hsieh and Klenow (2009) in defining a firm's (actual) physical productivity $TFPQ$ and revenue productivity $TFPR$ as¹⁰

$$TFPQ \equiv \frac{y}{(k^\alpha l^{1-\alpha})^\gamma} = (1 - \tau_a) (a^*)^{1-\gamma}$$

$$TFPR \equiv \frac{py}{k^\alpha l^{1-\alpha}}.$$

$TFPR$ captures firm-specific deviations from marginal product equalization, and is therefore useful as a measurement tool for the extent of capital misallocation in the economy.

¹⁰Although τ_a looks similar to the revenue distortion τ_y of Hsieh and Klenow (2009), it plays a different role in our setting. τ_a is a wedge between potential and actual physical productivity, reflecting the effect of lower schooling investments. τ_a is thus part of the definition of $TFPQ$, whereas τ_y would be part of the definition of $TFPR$, as in Hsieh and Klenow (2009). In fact, in our model there are no distortions akin to revenue distortions as defined by Hsieh and Klenow (2009).

From the optimality conditions

$$\begin{aligned}\gamma(1 - \alpha) \left(\frac{k}{l} \right)^\alpha TFP R &= w \\ \gamma \alpha \left(\frac{k}{l} \right)^{\alpha-1} TFP R &= (1 + \tau_k) (r + \delta),\end{aligned}$$

we obtain that revenue productivity

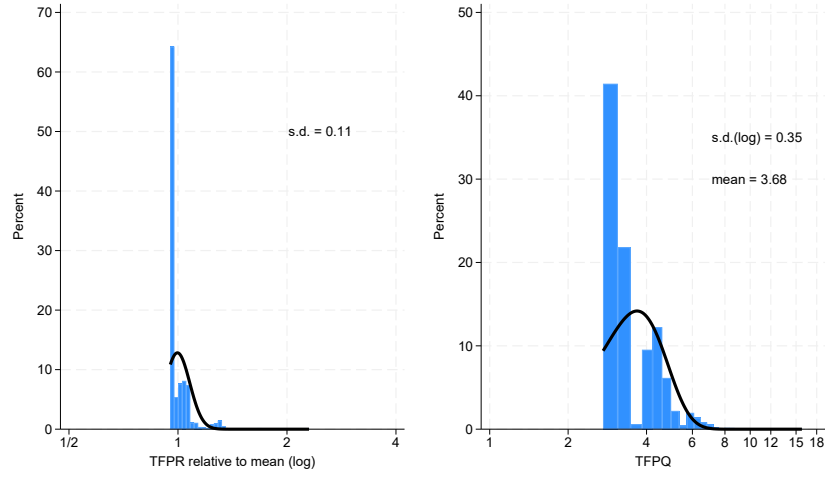
$$TFPR \propto (1 + \tau_k)^\alpha.$$

Absent frictions, $\tau_q^e = \tau_h^e = 0$ and $p_e = p_e^*$ for every individual. Therefore $\tau_a = \tau_k = 0$. In this case the distribution of $TFPR$ is degenerate, and the distribution of $TFPQ$ reflects only individual heterogeneity in abilities among households selecting into entrepreneurship. With frictions, the distribution of $TFPR$ becomes dispersed, reflecting physical capital misallocation, and the distribution of $TFPQ$ shifts to the left, reflecting lower levels of entrepreneurial human capital for constrained entrepreneurs. These features become more pronounced with a tighter capital constraint.

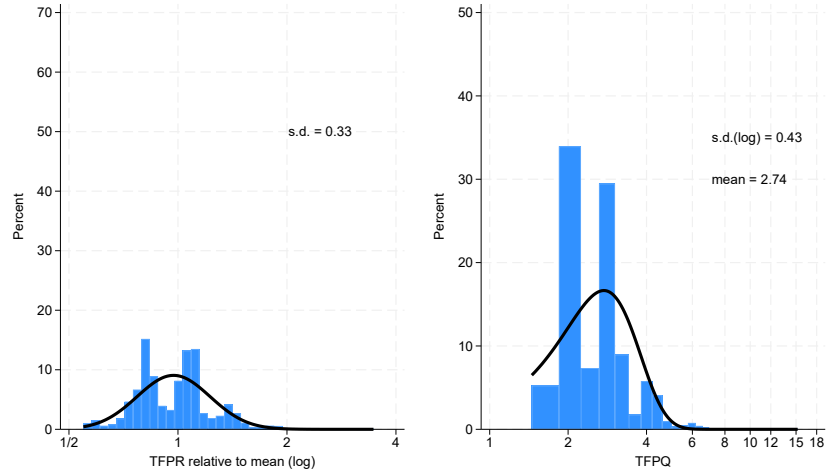
Figure 1 plots the distributions of $TFPR$ and $TFPQ$ in our model, for both the U.S. and the India (benchmark) calibrations. A tighter capital constraint in India generates significant misallocation and firm-level productivity effects. The standard deviation of $\log TFP R$ is three times higher in India, and average $TFP Q$ is about 25 percent lower.

3.4 Aggregate Productivity

Now we provide a connection between the distributions of $TFPR$ and $TFPQ$, and aggregate productivity. The final good sector admits an aggregate production



(a) TFPQ and TFPQ in the U.S.



(b) TFPQ and TFPQ in India

Figure 1: Revenue and physical productivity distributions in the model

function (see Appendix D):

$$Y = TFP \left(K^\alpha L^{1-\alpha} \right)^\gamma,$$

where $Y \equiv \int_M y d\Psi$, $K \equiv \int_M k d\Psi$, and $L \equiv \int_M l d\Psi$, with M the set of individual states selecting into entrepreneurship, and Ψ the cross-sectional distribution over individual states. Total factor productivity (TFP) is an aggregate of individual physical productivities and distortions

$$TFP \equiv \frac{\int_M a^* \left(\frac{1-\tau_a}{(1+\tau_k)^{\alpha\gamma}} \right)^{\frac{1}{1-\gamma}} d\Psi}{\left[\int_M a^* \left(\frac{1-\tau_a}{(1+\tau_k)^{1-\gamma+\alpha\gamma}} \right)^{\frac{1}{1-\gamma}} d\Psi \right]^{\alpha\gamma} \left[\int_M a^* \left(\frac{1-\tau_a}{(1+\tau_k)^{\alpha\gamma}} \right)^{\frac{1}{1-\gamma}} d\Psi \right]^{(1-\alpha)\gamma}}.$$

Defining

$$TFPR' \equiv TFPR (1 + \tau_k)^{\alpha(\gamma-1)} \propto (1 + \tau_k)^{\alpha\gamma}$$

we can rewrite aggregate TFP as

$$TFP = \int_M \left(TFPQ \frac{\overline{TFPR'}}{\overline{TFPR}} \right)^{\frac{1}{1-\gamma}} d\Psi, \quad (20)$$

where $\overline{TFPR'}$ is a geometric average of average marginal products of capital and labor.^{11,12} Expression (20) is identical to the one obtained in Hsieh and Klenow's (2009) accounting framework. We generalize it by considering distortions impacting firm-level physical productivity (τ_a).

To better understand the impact of distortions on aggregate TFP it is instructive to consider the case in which $(a^*)^{1-\gamma}$, $(1 - \tau_a)$, and $(1 + \tau_k)$ are jointly log-normally

¹¹The presence of decreasing returns to scale in production ($\gamma < 1$) introduces a slight difference between $TFPR$ and the weights on $TFPQ$ in the expression for TFP , which we define as $TFPR'$. The two quantities behave very similarly though.

¹² $\overline{TFPR'} \equiv \left\{ \left[\int_M \left(\frac{TFPQ}{\overline{TFPR'}} \right)^{\frac{1}{1-\gamma}} \frac{1}{1+\tau_k} d\Psi \right]^{\alpha} \left[\int_M \left(\frac{TFPQ}{\overline{TFPR'}} \right)^{\frac{1}{1-\gamma}} d\Psi \right]^{1-\alpha} \right\}^{\gamma(1-\gamma)} \kappa^{1-\gamma}$, with $\kappa \equiv \frac{1}{\gamma} \left(\frac{w}{1-\alpha} \right)^{1-\alpha} \left(\frac{r+\delta}{\alpha} \right)^{\alpha}$.

distributed across firms. The logarithm of aggregate TFP can then be written as a function of a few key moments of the joint distribution of firm-level wedges and potential productivities:

$$\log TFP = (1 - \gamma) \log ent + (1 - \gamma) \log \mathbb{E}_M \left[TFPQ^{\frac{1}{1-\gamma}} \right] - \frac{1}{2} \frac{\alpha \gamma (1 - \gamma + \alpha \gamma)}{1 - \gamma} \text{var}_M (\log TFPQ), \quad (21)$$

where $ent \equiv \int_M 1 d\Psi$ is the measure of the set of entrepreneurs, and the expectation and the variance are conditional on the states in this set. [Hsieh and Klenow \(2009\)](#) and [Midrigan and Xu \(2014\)](#) obtain very similar expressions, with two differences. First, since $\gamma = 1$ in their baseline case, the first term is absent. Second, and more importantly, in their case the $TFPQ$ distribution is exogenous. Here it is itself a function of the distortions generated by financial frictions, through the response of schooling investments. This response entails an amplification of the aggregate productivity effects of financial frictions, which go beyond capital misallocation. The endogenous feedback on the firm-level productivity distribution is therefore crucial for understanding the aggregate productivity effects of financial frictions.

The first term in equation (21) is the TFP gain from specialization. Since firm-level technology exhibits decreasing returns to scale, aggregate productivity rises when output is produced by a larger number of smaller firms. The other two terms in equation (21) illustrate two channels through which firm-level distortions reduce the aggregate TFP. First, τ_a decreases the average firm-level physical productivity, by introducing a gap between actual ($TFPQ$) and potential physical productivities ($(a^*)^{1-\gamma}$). This effect is due to lower human capital investments by the entrepreneurs in face of financial frictions. Second, dispersion in τ_k reduces aggregate TFP by introducing dispersion in marginal products of capital across firms, which is the

effect traditionally emphasized by the misallocation literature.

Decomposing further the second term in equation (21) allows us to identify five key moments that determine the total effect of financial frictions on aggregate TFP

$$\begin{aligned}
 \log TFP = & \underbrace{(1 - \gamma) \log ent}_{\text{Specialization}} + \underbrace{(1 - \gamma) \log \mathbb{E}_M a^*}_{\text{Potential productivity}} + \underbrace{(1 - \gamma) \log \mathbb{E}_M (1 - \tau_a)^{\frac{1}{1-\gamma}}}_{\text{Schooling under-investment}} \\
 & + \underbrace{\text{cov}_M (\log a^*, \log (1 - \tau_a))}_{\text{Schooling misallocation}} - \underbrace{\frac{1}{2} \frac{\alpha \gamma (1 - \gamma + \alpha \gamma)}{1 - \gamma} \text{var}_M (\log (1 + \tau_k))}_{\text{Capital misallocation}}.
 \end{aligned} \tag{22}$$

The first and the last terms are once more the specialization gain and physical capital misallocation effects. The total effect on firm-level productivity $\mathbb{E}_M TFPQ^{\frac{1}{1-\gamma}}$ is now decomposed into three elements.

The *potential productivity* term is determined by the selection of households into entrepreneurship, and thus by the misallocation of talent.¹³ In addition, it also reflects changes in entrepreneurial human capital investment due to changes in prices. The *schooling under-investment* term represents the effect of financial frictions on entrepreneurial investments in human capital. As this term shows, the average level of schooling distortions τ_a matters for aggregate TFP. The *schooling misallocation* term stems from the interaction between selection into entrepreneurship and human capital investments of entrepreneurs. A negative covariance between $\log a^*$ and $\log (1 - \tau_a)$ decreases aggregate TFP, since in this case entrepreneurs with the highest potential firm-level productivities face the largest distortions. In other words, the most talented entrepreneurs face the largest disincentive to invest in schooling, and therefore experience the largest productivity declines relative to potential.

¹³In reality, since all moments in the expression are conditional on the set of entrepreneurs M , they are all affected by misallocation of talent.

It is worth contrasting the aggregate productivity effects of the capital distortion τ_k and the productivity distortion τ_a . For the former, only the variance matters for aggregate productivity. In other words, cross-firm variation in gaps between marginal products and input prices are bad for input allocation, irrespective of them occurring in high or low productivity firms. Aggregate productivity could be increased by reallocating inputs to minimize this variance, independently from the average level of the gaps. The productivity distortion, instead, is capturing a different sort of problem, which is a gap between potential and actual productivity. In this case, the average level of the gaps matters, as does matter whether a given gap occurs in a high or a low potential productivity unit. For this reason, the corresponding mean and covariance terms are part of (22).

4 Schooling and entrepreneurial productivity: some evidence

A key ingredient of our theory is that human capital accumulation by entrepreneurs increases firm-level productivity. Two related implications are that more educated entrepreneurs run larger firms, and that they enjoy higher earnings. Cross-sectional heterogeneity in schooling, our model suggests, may stem from differences in either learning ability, entrepreneurial ability, or wealth. Our goal in this section is to present corroborating evidence showing that human capital is indeed positively associated to entrepreneurial outcomes. We abstract from the sources of variation in schooling, and an empirical assessment of causality.

Evidence is available for the U.S. from the NLSY79. Our starting point is [Levine and Rubinstein's \(2017\)](#) sample of individuals aged 25 and over between 1982 and 2012, with available information on employment status. Differently from them,

we restrict attention to the representative sample, and to self-employed individuals working full-time, full-year. We equate self-employment with entrepreneurship. We measure firm size with the number of workers, which includes the self-employed business owner in addition to all paid employees, and is available every other year starting in 2002. Earnings are CPI-deflated yearly wages plus income from business. Years of schooling is the number of years corresponding to the highest grade attained.

Table 1 contains the results. We start with the effect of entrepreneurial schooling on firm size. Our baseline regression in the first column is a straightforward firm size regression, with entrepreneurial schooling as the key determinant. Schooling has a significant impact on firm size, which is expected to increase by 4 percent for each additional year of schooling. Adding gender and race controls makes the coefficient on schooling barely insignificant at 10 percent. Many self-employment firms in our sample, however, only employ the business owner. This is consistent with [Levine and Rubinstein \(2017\)](#): these self-employed individuals run relatively basic unincorporated businesses, and tend to be much less educated than those that incorporate. This suggests that schooling might have a more significant effect along the extensive margin of firm size. In regression (3) we therefore run a simple linear probability model along the lines of regression (2), except that the dependent variable is now a dummy for whether the business has paid employees. In this case the coefficient on schooling is indeed positive and highly significant, suggesting the extensive margin to be the most significant and robust effect of entrepreneurial human capital on business size.

Regression (4) is a basic Mincerian earnings regression among entrepreneurs. We obtain a significant coefficient of about 11 percent. This magnitude is in line with what literature has found for workers and self-employed confounded ([Card, 1999](#)), although we make no attempt here to control for learning ability. Taken together, we interpret these findings as providing support for the main ingredient

Dependent variable:	number of workers (log) (1)	(2)	paid employees dummy (3)	earnings (log) (4)
years of schooling	0.0400 (0.089)	0.0387 (0.112)	0.0327 (0.002)	0.109 (0.000)
gender and non-white	no	yes	yes	yes
cubic experience	no	no	no	yes
industry dummies	yes	yes	yes	no
number of observations	990	990	990	3,497
R^2	0.184	0.189	0.093	0.169

Note: All regressions include year dummies. Industry dummies are for the main job, at the one-digit level (2000 Census). P-values in parenthesis based upon robust standard errors, clustered at the individual level.

Table 1: Schooling, firm size, and earnings premiums

in our model. They suggest schooling investments do play an important role for entrepreneurial outcomes, consistent with more educated entrepreneurs being more productive.

Our findings are related to a recent literature, following [Bloom and Reenen \(2007\)](#), which has been documenting a strong association between cross-firm differences in management practices and firm-level productivity levels. This literature has also uncovered some of the reasons behind the heterogeneity in firm management, like differences in manager's (or employees more generally) ability, but also differences in the extent of product market competition, and the interaction between firm-level "hard" technological factors and aggregate-level factors such as contract enforcement quality, social capital, or institutions favoring dynastic management, which may limit the scope of decision-making delegation and ultimately firm growth of more productive firms ([Bloom, Sadun and Reenen, 2016](#)). Our analysis abstracts from delegation, hence from the latter set of factors. In relation to this literature, our focus is on the role of inside management's ability for firm-level productivity, namely how it depends on formal schooling and its determinants.

5 Calibration

Our baseline strategy is similar to [Buera and Shin's \(2013\)](#) and several others, in the sense that we first calibrate the model economy to the U.S. and then vary the financial friction λ , holding the remaining parameters constant, in order to match India's ratio of external finance to output. We call this the *benchmark* India calibration.

We consider an alternative *schooling* calibration where we also allow the mean of the learning ability distribution, \bar{z} , to vary between the U.S and India, in order to match India's average years of schooling. The purpose of this exercise is to ask how far we can go in accounting for the U.S.-India differences in production outcomes, namely aggregate TFP, assuming we are able to account for schooling quantity differences.¹⁴ We view cross-country differences in \bar{z} not strictly speaking as differences in average learning ability, but as representing differences in school quality not captured by our modelling of current/within-cohort expenditures. These could be due to differences in school infrastructure (like buildings), to differences in school institutions (like school accountability and autonomy, public vs private mix), or even to differences in health infrastructure. All these factors affect how productive schooling inputs are in generating human capital. See [Hanushek and Woessmann \(2011\)](#) and [Woessmann \(2016\)](#) for a discussion.

Our baseline parameters are described in Table 2. The first-order Markov chain governing abilities is obtained from the discretization of a VAR(1) in logs where

$$\begin{aligned}\ln(z_{t+1}/\bar{z}) &= \rho_z \ln(z_t/\bar{z}) + \varepsilon_{t+1}^z, \\ \ln(x_{t+1}/\bar{x}) &= \rho_x \ln(x_t/\bar{x}) + \varepsilon_{t+1}^x,\end{aligned}$$

¹⁴Although a lower \bar{z} in India mechanically lowers TFP, our focus is not on this effect but rather on the entrepreneurial schooling responses. As we make clear in Section 6, these effects alone are quantitatively more important with lower \bar{z} .

and the disturbances are normally distributed with variance-covariance matrix

$$\Sigma = \begin{pmatrix} \sigma_z^2 & \sigma_{zx} \\ \sigma_{zx} & \sigma_x^2 \end{pmatrix}.$$

We employ the procedure described by [Tauchen and Hussey \(1991\)](#), with 15 states for entrepreneurial ability and 4 states for learning ability.

One model period is 30 years. Individuals start life at age 6. From age 6 until age 36 (childhood) is the period when schooling and early working in the labor market take place. From age 36 until retirement age 66 (adulthood) is the period when the main economic activity, entrepreneurship or working for a wage, takes place.

Some parameters are calibrated externally to the model. These are in the top block of Table 2. The coefficient of relative risk aversion belongs to the interval of available estimates, and is a standard value in quantitative analysis, as is the rate of physical capital depreciation. The parameters governing the income share of capital (α) and the income share of entrepreneurial income (γ) are also standard in models of entrepreneurship (see for example [Atkeson and Kehoe, 2005](#), who base their calibration on a survey of direct estimates, as well as [Restuccia and Rogerson, 2008](#), [Buera and Shin, 2013](#), and [Midrigan and Xu \(2014\)](#)).¹⁵ We set the autocorrelation coefficient of learning ability to the intergenerational correlation coefficient of IQ scores reported by [Bowles and Gintis \(2002\)](#), between the average parental and the average offspring IQ scores. Finally, we impose an upper bound on schooling time corresponding to 20 years of formal schooling.

The remaining 14 parameters are chosen in order to minimize the sum of squared percentage deviations of 14 data moments from their model analogues. The bottom

¹⁵Given decreasing returns to scale, income accrues to capital, labor, and the entrepreneurial input. We attribute the latter to capital and labor incomes, in shares α and $1 - \alpha$ respectively. We therefore equate α to the aggregate capital income share value.

Table 2: Benchmark calibration

Parameter	Value	Target	Model	Data
<i>External calibration</i>				
σ	1.0	direct estimates		
δ	0.844	yearly depreciation rate of 6%		
α	1/3	capital income share		
γ	0.85	direct estimates		
ρ_z	0.72	intergenerational correlation of IQ scores		
\bar{s}	2/3	up to 20 years of formal schooling (ages 6-26)		
<i>Internal calibration</i>				
β	0.205	yearly real interest rate	0.036	0.04
\bar{z}	26.0	average years of schooling among entrepreneurs	14.2	13.6
ξ	0.965	average years of schooling among workers	13.7	14.1
σ_z	0.138	earnings share of top 5%	0.36	0.35
\bar{x}	0.837	Mincerian returns to schooling among entrepreneurs	0.117	0.109
η	0.67	output share of schooling expenditures	0.082	0.105
\bar{l}	2.89	output share of teacher and staff compensation	0.03	0.05
ψ	0.6	average labor earnings at age 46 over average at age 26	1.73	1.75
ρ_x	0.45	intergenerational correlation of entrepreneurship	0.27	0.32
σ_x	0.28	employment share of top 5% establishments	0.59	0.57
$\sigma_{z,x}$	-0.107	ratio of median earnings (entrepreneurial over labor)	1.15	1.11
ϕ	0.0041	share of household credit in total external finance	0.18	0.19
$\lambda_{U.S.}$	35.0	ratio of external finance to output (U.S.)	2.42	2.91
λ_{India}	1.345	ratio of external finance to output (India)	0.46	0.46

block of Table 2 shows the values for these parameters, as well as how model's moments compare to the data. As is common in this type of analysis, we identify each parameter with a moment which we believe is particularly helpful in identifying it, although in the end all parameters are jointly determined through a fairly complex system of nonlinear equations.

When computing the moments in the model we assume a survey protocol that mimics the data, where individuals are interviewed every year while labor force

participants. Due to schooling time, young workers are therefore interviewed less often than either adult workers or entrepreneurs. We also take one entrepreneurial firm in the model as corresponding to an establishment in the data.¹⁶

We comment on each of the moments we have selected. A yearly real interest rate of 4 percent is roughly between the real return on riskless bonds and the real return on equity over a long horizon. Based upon the NLSY79 data of Section 4, we compute three summary statistics: around 14 average years of schooling for both self-employed (our notion of entrepreneurs) and salaried workers and a ratio between the median annual earnings among self-employed to the median across salaried workers of 1.11. The latter moment is key in identifying a slightly negative covariance between innovations to learning and entrepreneurial abilities. Meaning that households with high learning ability tend to have a slight disadvantage at entrepreneurship. Otherwise entrepreneurs would have much higher earnings relative to workers, compared to the data. We also use our estimate of the Mincerian returns to schooling among entrepreneurs from Table 1.

For the output shares of (public and private) schooling expenditures and teacher and staff compensation we use the same numbers as Erosa, Koreshkova and Restuccia (2010). These are based upon total expenditure data for 1990-1995 from the U.S. Department of Education, together with an estimate of the share of teacher and staff compensation from the OECD. The ratio of average labor earnings at age 46 over age 26 comes from Figure 1 of Kambourov and Manovskii (2009). It is based upon the PSID (Panel Study of Income Dynamics) and refers to the cohort entering the labor market in 1968. The intergenerational correlation of entrepreneurial occupation is reported by Dunn and Holtz-Eakin (2000), and corresponds to the fraction of

¹⁶This is in line with the related literature, namely Buera, Kaboski and Shin (2011), Buera and Shin (2013), and Midrigan and Xu (2014). Our choice of calibration targets reflects this view. We acknowledge the caveat that, in the data, there exist multi-establishment firms, and more importantly firms whose ownership does not coincide with management, or more generally self-employment.

sons of self-employed fathers in the NLS (National Longitudinal Surveys) who were themselves self-employed at some point in the sample.

The employment share of the top 5 percent establishments is reported by [Henly and Sanchez \(2009\)](#), based upon the U.S. Census County Business Pattern series. This figure is across establishments in all sectors of activity in the year 2006. The earnings share of the top 5 percent comes from [Díaz-Giménez, Glover and Ríos-Rull \(2011\)](#) and is based on the Survey of Consumer Finances.

The ratio of total external finance (including private credit) to output in the U.S. was obtained from the 2013 update of the [Beck, Demirgüç-Kunt and Levine \(2000\)](#) financial indicators database. We adjusted the reported stock market capitalization by the average book-to-market ratio, following [Buera, Kaboski and Shin \(2011\)](#). Our number is the average over the years 1990-2011. Our other financial market indicator is the share of household credit in total external financing. We obtained it as the product between the share of household credit in total credit in 2005 from the [International Monetary Fund \(2006\)](#), and the share of total credit in total external financing from the 2013 update of the [Beck, Demirgüç-Kunt and Levine \(2000\)](#) data set, again averaged over the years 1990-2011.

For the benchmark India calibration, a value of $\lambda_{India} = 1.345$ allows us to match exactly India's ratio of external finance to output, obtained as described previously for the U.S. In our schooling India calibration (not reported in Table 2) we obtain $\lambda_{India} = 1.291$, and $\bar{z}_{India} = 8.691$. With these parameters, we can again match exactly India's the ratio of external finance to output and average schooling of 5.95 years (see Table 6 for schooling).

We now comment on our reliance on a two-period overlapping-generations model in order to quantify the effects of financial frictions. [Buera, Kaboski and Shin \(2011\)](#) discuss the potential pitfalls of this sort of analysis, which they find tends to minimize the role of self-financing. The argument is that a higher frequency multi-

period environment is needed in order to allow firms to grow out of the financial constraints, given persistent productivity levels.¹⁷ Although we acknowledge this would be ideal, such approach is unfortunately very costly here: the multi-period nature of both human capital accumulation (by the child) and entrepreneurship (by the parent) would imply a large increase in the state-space. We believe our dynastic environment offers a reasonable compromise. Note that [Buera, Kaboski and Shin \(2011\)](#) consider non-altruistic agents in their two-period model, born with no wealth, and leaving no bequests. In contrast, we work with a dynastic environment with full altruism and unrestricted bequests. These inter-generational links, together with the fact that ability is persistent over generations, give opportunity for high-ability dynasties to grow out of the financial constraints. This element mitigates the usual concern with two-period overlapping-generations models. Further, in our model agents may self-finance further within a generation, by cutting back on entrepreneurial schooling investments - the central mechanism we emphasize.

6 Aggregate Consequences of Financial Frictions

We now consider the aggregate consequences of frictions in the model, for the U.S. and the two India calibrations, benchmark (only λ differs from the U.S.) and schooling (both λ and \bar{z} differ from the U.S.). Table 3 looks at the implications for aggregate output, capital-output ratios, and aggregate TFP, both in the model and in the data. Our data source is version 8.1 of the Penn World Tables ([Feenstra, Inklaar and Timmer, 2015](#)). Appendix E describes in detail the mapping of the aggregate production function variables between model and data.

The model produces significant differences in macro aggregates. The magni-

¹⁷Implicit in this reasoning is a problem of lack of time-aggregation, i.e. a properly calibrated 30-year model like we have here might not necessarily correspond to the time aggregation of a higher frequency model.

		Y		K/Y		TFP	
		Model	Data	Model	Data	Model	Data
U.S.		1.00	1.00	2.16	2.99	1.00	1.00
India	bench	0.46	0.08	1.57	1.93	0.73	0.26
	school	0.05		1.74		0.50	

Table 3: Macroeconomic aggregates

tudes are smaller than what we see in the data for the benchmark (‘bench’) calibration, but much closer for the schooling (‘school’) calibration. Under the benchmark calibration, the model accounts for 36 percent of the measured 74 percent India-U.S. TFP difference, and for 59 percent of the measured 92 percent aggregate output difference. Under the schooling calibration, it accounts for 68 percent of the measured TFP difference, and generates an output difference about as large as in the data.¹⁸

Table 4 provides a decomposition of the model-implied TFP difference, in line with equation (22). That is, we compute the basic wedges in the model and plug them in (22). As discussed previously, this approach is appropriate only to the extent that joint log-normality is a good approximation. We find that, while the model-implied TFP differences (Table 3) do appear to be reasonably approximated by the TFP differences computed from (22), the errors are nevertheless not entirely negligible (see bottom of Table 4). Our decomposition results are therefore subject to this caveat.

According to this decomposition, the *specialization* term contributes negatively to the U.S.-India TFP difference, since the entrepreneurship rate is higher in India. The other two terms, *firm-level productivity* and *physical capital misallocation*,

¹⁸The reason the latter calibration delivers output differences in line with the data in spite of lower TFP differences (and similar capital-output ratios) is that human capital stock differences turn out to be larger in the model than the PWT8.1 estimates we rely upon to compute TFP - see Appendix E - even if we do match average years of schooling differences. See also the discussion surrounding Table 6.

contribute each to over a 16 percent TFP difference under the benchmark calibration. Our model produces TFP losses from capital misallocation which are a bit higher than those in Midrigan and Xu's (2014) model calibrated to Korea, which tend to stay below 10 percent, but significantly lower than those reported by Hsieh and Klenow (2009), which can be as high as 60 percent. Like in Midrigan and Xu (2014), entrepreneurs adjust to the presence of financial frictions by relying more on self-financing. In our model, this happens while entrepreneurs cut back on schooling investments and spend a larger fraction of their early lives working for a wage, mitigating the quantitative role for capital misallocation.

The contribution of *firm-level productivity* is further decomposed into three terms. *Potential productivity* is on average higher in India, since input prices are lower, in spite of a worse ability selection into entrepreneurship. Lower input prices give incentives for unconstrained entrepreneurs to expand their production scale, and hence invest more in education. A lower interest rate also encourages entrepreneurs to invest more in education, for given production scale. This term therefore contributes negatively to the model-implied U.S.-India TFP difference. However, *schooling under-investment* is more important in India, contributing to a 20.3 percent TFP loss. Finally, there is also a significantly higher degree of *schooling misallocation* in India: the most talented entrepreneurs are the ones cutting back the most in terms of education, and this effect entails a 14 percent TFP loss. Taken together, schooling under-investment and schooling misallocation are the most important drivers of India's model-implied TFP loss.

The firm-level productivity effect is significantly larger under the schooling calibration, accounting in this case for a 48 percent TFP loss in India. One of the main effects, not surprisingly, comes from what is now a 7 percent loss in potential productivity. This is due to the direct productivity effect of a lower \bar{z} , compounded by lower schooling investments conditional on the U.S. level of financial frictions.

We do not wish to emphasize with this experiment that TFP in India is lower simply due to the mechanical direct effect of a lower \bar{z} . We wish to emphasize instead that higher frictions in India play a much more significant role when \bar{z} is low: schooling under-investment contributes to a TFP loss which is twenty percent larger, and schooling misallocation four times larger.

It is possible to obtain a back-of-the-envelope figure for India's TFP loss under the schooling calibration which nets out the mechanical direct effect of a lower \bar{z} . According to our calibration, this direct effect amounts to a $1 - (\bar{z}^{IND} / \bar{z}^{US})^{1-\gamma} = 15.2$ percent TFP loss. Without this effect, the potential productivity loss term can be approximated to $6.8 - 15.2 = -8.4$ percent, actually a gain.¹⁹ In this case, the total TFP loss in India would still be 39.6 percent, only a bit lower than the full 48.1 percent. We conclude that the model's measure of success under the schooling calibration, the ability to account for 68 percent of the measured India-U.S. TFP difference, is not driven by the mechanical effect of a lower \bar{z} .²⁰

The intuition behind these larger effects can be traced back to the discussion surrounding the expression for the productivity wedge τ_a in equation (19). The productivity of human capital investments in India is on average lower under the schooling calibration. This effectively weakens the self-financing channel for fu-

¹⁹Potential productivity captures direct, as well as some indirect effects of a lower \bar{z} in India: h^* decreases induced by lower schooling inputs, h^* increases induced by lower input prices, and a^* decreases due to a more adverse talent misallocation. The fact that we obtain a gain means the effect of lower input prices is dominant, similarly to the benchmark calibration.

²⁰It is worth comparing our TFP results with the related quantitative literature. Buera and Shin (2013) and Buera, Kaboski and Shin (2011) and are among the closest papers. Going from the perfect credit markets to financial autarky, the TFP losses are estimated to be 24 percent in the former (which features exogenously-given firm-level taxes/subsidies) and 36 percent in the latter (which features cross-sectoral variation in fixed costs). Midrigan and Xu (2014) also estimate TFP losses up to 26 percent from shutting down external finance relative to a Korean calibration, in a framework with entry into entrepreneurship and the possibility of technology adoption. Our estimates are therefore generally higher than in the literature. The comparison, however, is not straightforward, given different model features, calibrations, and range of variation of the severity of financial frictions. Financial frictions may well generate even larger TFP effects if we extended our model to feature some of the ingredients emphasized by these different papers.

ture entrepreneurs, by lowering their first-period wage earnings. For given basic distortions τ_q^e and τ_h^e , a lower ability to raise first-period earnings makes schooling investments more expensive. This mechanism amplifies schooling under-investments in India, and generates individual-level productivity distortions τ_a which are higher on average, as well as more dispersed across individuals. This impacts the schooling under-investment and misallocation terms of equation (22) leading to the larger effects displayed in Table 4.

<i>TFP</i> term	% Loss India relative to U.S.	
	bench	school
Specialization	−14.8	−21.6
Firm-level productivity	+17.0	+47.4
Potential productivity	−21.0	+6.8
Schooling under-investment	+20.3	+31.4
Schooling misallocation	+14.0	+17.8
Physical capital misallocation	+16.2	+18.7
Approximate <i>TFP</i>	20.0	48.1
Model <i>TFP</i>	26.6	49.5

Note: Entries are percent changes for each term of equation (22) written in levels, rather than logs. The reported overall effects may therefore be recovered as the product of the partial effects.

Table 4: Aggregate TFP loss decomposition

The next two sets of results provide a simple illustration of how well our model does in matching certain micro-level production and schooling outcomes. Table 5 focuses on production. It displays the rate of entrepreneurship and the average firm size (relative to the U.S).

The rate of entrepreneurship in the U.S. is based upon the data from Section 4. For India, we rely on information from Ministry of Statistics and Programme Implementation (2014).²¹ Entrepreneurs are household heads reporting to be self-

²¹All Indian data used throughout the paper is available at <https://www.mospi.gov.in/>.

employed, and workers includes both salaried and casual labor. We report numbers for ages 15-59, and across all genders, sectors, and regions.

		ent.rate		avg. firm size	
		Model	Data	Model	Data
U.S.		4.8	9.2	1.00	1.00
India	bench	12.0	48.6	0.38	0.29
	school	17.7		0.26	

Table 5: Entrepreneurship rate and average firm size

In the data, our measure of size is the number of paid employees.²² Once again, we take the data counterpart of an entrepreneurial firm in the model to be an establishment. For the U.S., the evidence comes from [Henly and Sanchez \(2009\)](#), based on the Census Bureau’s 2006 County Business Pattern Series. They report an average of 15 employees per establishment across all sectors of activity (their Figure 1). For India, we rely on the Fifth Economic Census by the Indian Ministry of Statistics and Programme Implementation, which concerns the year 2005. The data is available for all sectors of activity across all Indian states, in both urban and rural settings. It provides the same type of information (i.e. establishment and worker counts by establishment size groups, for establishments with hired workers) as the County Business Pattern Series in the U.S. This allows us to apply the same method as [Henly and Sanchez \(2009\)](#) to obtain approximations to the relevant moments of the size distribution in India from the establishment and worker counts, and ensures comparability across the two countries. We obtain an average of 4.38 employees per establishment in India, implying a India-U.S. ratio of 0.29 in the data.

Consistently with the data, our model generates more entrepreneurs in India,

²²We use the total firm-level labor input as the model counterpart. Unfortunately our model does not distinguish between the number of workers and the quantity of human capital employed. To partially address this issue, we equate the number of workers employed by a firm to $\max\{l/\bar{h}^w, 1\}$, where \bar{h}^w is the average level of human capital per worker in the whole economy.

operating on average at a smaller scale. The main mechanism driving the higher rate of entrepreneurship is the drop in input prices, which encourages lower ability individuals to engage in production. The magnitude, however, is much lower than in the data.²³

Overall, we can say that the model delivers firm-size distribution differences which are consistent with the data. The model accounts for 76 percent of the 2/3 India-U.S. difference in average firm size under the benchmark calibration, and nearly matches that difference under the schooling calibration.

Table 6 looks at average years of schooling. The U.S. data, aggregate and by occupation, are the NLSY79 used in our calibration. For India, we again rely on Ministry of Statistics and Programme Implementation (2014), and focus on population aged 15–59 between 2011 and 2012, across all sectors and regions, including regular and casual workers.

		aggregate		workers		entrepreneurs	
		Model	Data	Model	Data	Model	Data
U.S.		13.72	14.03	13.70	14.07	14.17	13.63
India	bench	13.33		13.50		12.13	
	school	5.93	5.95	6.51	6.11	3.24	5.79

Table 6: Years of schooling

The model produces lower schooling levels in India independent of occupation, but my much less than in the data under the benchmark calibration. The main reason the model is unable to deliver a larger effect is that the interest rate is lower in India, which incentivizes larger schooling investments.²⁴

²³If we exclude agriculture from the data, in an extreme attempt to deal with the large importance of subsistence farming in India, we still obtain an entrepreneurship rate of 37.8%. Such high self-employment rates are most likely an artifact: the data counts helpers in family business as self-employed, in addition to own-account workers and employers.

²⁴The cross-country variation in schooling time is also lower than in the data in Erosa, Koreshkova

The schooling calibration matches the average years of schooling in India by design, and therefore produces much larger schooling responses across occupations as well. The effect is more pronounced across entrepreneurs, highlighting our central mechanism. Such large gap in schooling outcomes is associated with a large degree of schooling distortions, and a large aggregate TFP effect. Our key message: understanding educational outcomes is crucial for understanding production outcomes.

7 Concluding Remarks

We investigate the aggregate productivity effects of financial frictions, in an environment where frictions impact both firm-level investment decisions, and household-level schooling decisions. We show that, in anticipation of the effect credit constraints have on their future business activity, entrepreneurs under-invest in schooling. Further, this behavior is more pronounced among the most able entrepreneurs, generating a misallocation of schooling investments. Both effects are shown to produce important aggregate productivity losses, ranging from 36 to 68 percent of the U.S.-India aggregate productivity difference. These findings imply that schooling distortions are a major source of productivity differences. Our research suggests educational policies, such as tuition subsidies or public provision of schooling, may have significant productivity effects. Analyzing the role of such policies in reducing misallocation and improving production outcomes is a natural and interesting direction for further work.

and Restuccia (2010), see their Figure 3. They argue that their human capital accumulation environment, same as ours, tends to understate cross-country schooling time differences, while at the same time generating large quality differences. Our model produces similar implications under the benchmark calibration.

References

- Amaral, Pedro S., and Erwan Quintin.** 2010. "Limited Enforcement, Financial Intermediation, And Economic Development: A Quantitative Assessment." *International Economic Review*, 51(3): 785–811.
- Atkeson, Andrew, and Patrick Kehoe.** 2005. "Modeling and Measuring Organizational Capital." *Journal of Political Economy*, 113: 1026–1053.
- Barro, Robert, and Jong-Wha Lee.** 1993. "International Comparisons of Educational Attainments." *Journal of Monetary Economics*, 32: 363–94.
- Bartelsman, Eric, John Haltiwanger, and Stefano Scarpetta.** 2013. "Cross-Country Differences in Productivity: The Role of Allocation and Selection." *American Economic Review*, 103(1): 305–34.
- Beck, Thorsten, Asli Demirgüç-Kunt, and Ross Levine.** 2000. "A New Database on Financial Development and Structure." *World Bank Economic Review*, 14: 597–605.
- Bhattacharya, Dhritman, Nezih Guner, and Gustavo Ventura.** 2013. "Distortions, Endogenous Managerial Skills and Productivity Differences." *Review of Economic Dynamics*, 16(1): 11–25.
- Bloom, Nicholas, and John Van Reenen.** 2007. "Measuring and Explaining Management Practices Across Firms and Countries." *The Quarterly Journal of Economics*, 122(4): 1351–1408.
- Bloom, Nicholas, Raffaella Sadun, and John Van Reenen.** 2016. "Management as a Technology?" National Bureau of Economic Research, Inc NBER Working Papers 22327.
- Bowles, Samuel, and Herbert Gintis.** 2002. "The Inheritance of Inequality." *Journal of Economic Perspectives*, 16(3): 3–30.
- Buera, Francisco J., and Yongseok Shin.** 2013. "Financial Frictions and the Persistence of History: A Quantitative Exploration." *Journal of Political Economy*, 121(2): 221 – 272.
- Buera, Francisco J., Joseph P. Kaboski, and Yongseok Shin.** 2011. "Finance and Development: A Tale of Two Sectors." *American Economic Review*, 101(5): 1964–2002.

- Card, David.** 1999. "The causal effect of education on earnings." In *Handbook of Labor Economics*. Vol. 3 of *Handbook of Labor Economics*, , ed. O. Ashenfelter and D. Card, Chapter 30, 1801–1863. Elsevier.
- Caselli, Francesco.** 2005. "Accounting for Cross-Country Income Differences." In *Handbook of Economic Growth*. Vol. 1 of *Handbook of Economic Growth*, , ed. Philippe Aghion and Steven Durlauf, Chapter 9, 679–741. Amsterdam, New York and Oxford:Elsevier Science, North Holland.
- Castro, Rui, Gian Luca Clementi, and Glenn MacDonald.** 2004. "Investor Protection, Optimal Incentives, and Economic Growth." *Quarterly Journal of Economics*, 119(3): 1131–1175.
- Castro, Rui, Gian Luca Clementi, and Glenn MacDonald.** 2009. "Legal Institutions, Sectoral Heterogeneity, and Economic Development." *Review of Economic Studies*, 76(2): 529–561.
- Clausen, Andrew, and Carlo Strub.** 2013. "A General and Intuitive Envelope Theorem." University of Pennsylvania.
- Cole, Harold L., Jeremy Greenwood, and Juan M. Sanchez.** 2016. "Why Doesn't Technology Flow From Rich to Poor Countries?" *Econometrica*, 84: 1477–1521.
- Córdoba, Juan Carlos, and Marla Ripoll.** 2013. "What explains schooling differences across countries?" *Journal of Monetary Economics*, 60(2): 184–202.
- Dunn, Thomas, and Douglas Holtz-Eakin.** 2000. "Financial Capital, Human Capital, and the Transition to Self-Employment: Evidence from Intergenerational Links." *Journal of Labor Economics*, 18(2): 282–305.
- Díaz-Giménez, Javier, Andrew Glover, and José-Víctor Ríos-Rull.** 2011. "Facts on the distributions of earnings, income, and wealth in the United States: 2007 update." *Quarterly Review*, 34(1): 2–31.
- Erosa, Andres, and Ana Hidalgo-Cabrillana.** 2008. "On Finance As A Theory Of TFP, Cross-Industry Productivity Differences, And Economic Rents." *International Economic Review*, 49(2): 437–473.
- Erosa, Andres, Tatyana Koreshkova, and Diego Restuccia.** 2010. "How Important is Human Capital? A Quantitative Theory Assessment of World Income Inequality." *Review of Economic Studies*, 77(4): 1421–1449.
- Evans, David, and Boyan Jovanovic.** 1989. "An estimated model of entrepreneurial choice under liquidity constraints." *Journal of Political Economy*, 97: 808–27.

- Feenstra, Robert C., Robert Inklaar, and Marcel P. Timmer.** 2015. "The Next Generation of the Penn World Table." *American Economic Review*, 105(10): 3150–3182. available for download at www.ggdc.net/pwt.
- Foster, Lucia, John Haltiwanger, and Chad Syverson.** 2008. "Reallocation, Firm Turnover, and Efficiency: Selection on Productivity or Profitability?" *American Economic Review*, 98(1): 394–425.
- Galor, Oded, and Joseph Zeira.** 1993. "Income Distribution and Macroeconomics." *Review of Economic Studies*, 60(1): 35–52.
- Greenwood, Jeremy, Juan Sanchez, and Cheng Wang.** 2013. "Quantifying the Impact of Financial Development on Economic Development." *Review of Economic Dynamics*, 16(1): 194–215.
- Hall, Robert E., and Charles I. Jones.** 1999. "Why Do Some Countries Produce So Much More Output Per Worker Than Others?" *The Quarterly Journal of Economics*, 114(1): 83–116.
- Hanushek, Eric A., and Ludger Woessmann.** 2011. "The Economics of International Differences in Educational Achievement." , ed. Erik Hanushek, Stephen Machin and Ludger Woessmann Vol. 3 of *Handbook of the Economics of Education*, Chapter 2, 89–200. Elsevier.
- Henly, Samuel E., and Juan M. Sanchez.** 2009. "The U.S. establishment-size distribution: secular changes and sectoral decomposition." *Economic Quarterly*, 95(4): 419–454.
- Hsieh, Chang-Tai, and Peter J. Klenow.** 2009. "Misallocation and Manufacturing TFP in China and India." *The Quarterly Journal of Economics*, 124(4): 1403–1448.
- Hsieh, Chang-Tai, and Peter J. Klenow.** 2010. "Development Accounting." *American Economic Journal: Macroeconomics*, 2(1): 207–23.
- International Monetary Fund.** 2006. *Global Financial Stability Report: Market Developments and Issues*. Washington, DC:International Monetary Fund.
- Jeong, Hyeok, and Robert Townsend.** 2007. "Sources of TFP growth: occupational choice and financial deepening." *Economic Theory*, 32(1): 179–221.
- Kambourov, Gueorgui, and Iouri Manovskii.** 2009. "Accounting for the Changing Life-Cycle Profile of Earnings." University of Toronto.

- Kehoe, Timothy J., and David K. Levine.** 1993. "Debt-Constrained Asset Markets." *Review of Economic Studies*, 60(4): 865–888.
- Klenow, Peter J., and Andrés Rodríguez-Clare.** 1997. "The Neoclassical Revival in Growth Economics: Has It Gone Too Far?" In *NBER Macroeconomics Annual 1997*. Vol. 12, 73–103. Cambridge, MA:MIT Press.
- Levine, Ross, and Yona Rubinstein.** 2017. "Smart and Illicit: Who Becomes an Entrepreneur and Do They Earn More?" *The Quarterly Journal of Economics*, 132(2): 963–1018.
- Lochner, Lance J., and Alexander Monge-Naranjo.** 2011. "The Nature of Credit Constraints and Human Capital." *American Economic Review*, 101(6): 2487–2529.
- Manuelli, Rodolfo E., and Ananth Seshadri.** 2014. "Human Capital and the Wealth of Nations." *American Economic Review*, 104(9): 2736–62.
- Mestieri, Marti, Johanna Schauer, and Robert Townsend.** 2017. "Human Capital Acquisition and Occupational Choice: Implications for Economic Development." *Review of Economic Dynamics*, 25: 151–186.
- Midrigan, Virgiliu, and Daniel Yi Xu.** 2014. "Finance and Misallocation: Evidence from Plant-Level Data." *American Economic Review*, 104(2): 422–58.
- Ministry of Statistics and Programme Implementation.** 2014. "Employment and Unemployment Situation in India, July 2011-June 2012." *Government of India, National Sample Survey Office, 68th round*.
- Moll, Benjamin.** 2014. "Productivity Losses from Financial Frictions: Can Self-Financing Undo Capital Misallocation?" *American Economic Review*, 104(10): 3186–3221.
- Moll, Benjamin, Robert M. Townsend, and Victor Zhorin.** 2017. "Economic development, flow of funds, and the equilibrium interaction of financial frictions." *Proceedings of the National Academy of Sciences*, 114(24): 6176–6184.
- Restuccia, Diego, and Richard Rogerson.** 2008. "Policy Distortions and Aggregate Productivity with Heterogeneous Plants." *Review of Economic Dynamics*, 11(4): 707–720.
- Tauchen, George, and Robert Hussey.** 1991. "Quadrature-Based Methods for Obtaining Approximate Solutions to Nonlinear Asset Pricing Models." *Econometrica*, 59(2): 371–96.

Woessmann, Ludger. 2016. “The Importance of School Systems: Evidence from International Differences in Student Achievement.” *Journal of Economic Perspectives*, 30(3): 3–32.

Appendix

A Competitive Equilibrium

Definition. A stationary recursive competitive equilibrium is a set of value functions $v^w(\omega, z, x)$, $v^e(\omega, z, x)$, and $v(\omega, z, x)$, together with the associated decision rules, a set of entrepreneurial households M , prices w and r , and an invariant distribution over household states Ψ such that given prices,

- $v^w(\omega, z, x)$ and $v^e(\omega, z, x)$ solve problems (P w) and (P e), respectively, and $v(\omega, z, x)$ solves (10),
- the set of entrepreneur-households is defined by:

$$M = \{(\omega, z, x) \in S \mid v^e(\omega, z, x) > v^w(\omega, z, x)\},$$

where $S \subseteq \mathbb{R} \times \mathbb{R}_+^2$ is the individual household's state space,

- market for labor clears:

$$\int_M l d\Psi + \int_S s \bar{l} d\Psi = \int_{S \setminus M} h d\Psi + \int_S (1 - s) \psi h d\Psi,$$

- market for capital clears:

$$\int_M k d\Psi = \int_S \frac{q}{1 + r} d\Psi,$$

- market for goods clears:

$$\int_S c d\Psi + \int_S e d\Psi + \delta \int_M k d\Psi = \int_M x h^{1-\gamma} (k^\alpha l^{1-\alpha})^\gamma d\Psi,$$

- distribution Ψ is invariant and defined by:

$$\Psi(\hat{S}) = \int_S P(X, \hat{S}) d\Psi(X) \text{ for all } \hat{S} \in \mathcal{B}_S,$$

where $P : S \times \mathcal{B}_S \rightarrow [0, 1]$ is a transition function generated by the decision rules and the stochastic processes for z and x , and \mathcal{B}_S is the Borel σ -algebra of subsets of S .

B Profit Functions

The solution to the profit maximization problem is, for unconstrained entrepreneurs ($q \geq q^*(h, x)$, where $q^*(h, x) \equiv (1+r)k^*/\lambda$):

$$\begin{aligned} k^* &= \left[\frac{(1-\alpha)(r+\delta)^{1-\frac{1}{(1-\alpha)\gamma}}}{\alpha w} \right]^{(1-\alpha)\frac{\gamma}{1-\gamma}} (\alpha\gamma)^{\frac{1}{1-\gamma}} a \\ l^* &= \frac{(1-\alpha)(r+\delta)}{\alpha w} k^* \\ y^* &= a^{1-\gamma} \left((k^*)^\alpha (l^*)^{1-\alpha} \right)^\gamma \\ \Pi^*(h, x) &= y^* - wl^* - (r+\delta)k^* \equiv Aa, \end{aligned}$$

and for constrained entrepreneurs ($q < q^*(h, x)$):

$$\begin{aligned} k^c &= \max \left\{ \lambda \frac{q}{1+r}, 0 \right\} \\ l^c &= \left[\frac{\gamma(1-\alpha)(k^c)^{\alpha\gamma}}{w} a^{1-\gamma} \right]^{\frac{1}{1-(1-\alpha)\gamma}} \\ y^c &= a^{1-\gamma} \left((k^c)^\alpha (l^c)^{1-\alpha} \right)^\gamma \\ \Pi^c(q, h, x) &= y^c - wl^c - (r+\delta)k^c \\ &\equiv B(q) a^{\frac{1-\gamma}{1-(1-\alpha)\gamma}} - (r+\delta) \frac{\lambda}{1+r} q, \end{aligned}$$

where

$$\begin{aligned} A &= \left[A_0 \left(\frac{(1-\alpha)(r+\delta)}{\alpha w} \right)^{1-\alpha} \right]^\gamma (1-\gamma) \\ A_0 &= \left[\frac{(1-\alpha)(r+\delta)^{1-\frac{1}{(1-\alpha)\gamma}}}{\alpha w} \right]^{(1-\alpha)\frac{\gamma}{1-\gamma}} (\alpha\gamma)^{\frac{1}{1-\gamma}} \\ B(q) &= B_0 (q^{\alpha\gamma})^{\frac{1}{1-(1-\alpha)\gamma}} \\ B_0 &= \frac{1-(1-\alpha)\gamma}{(1-\alpha)\gamma} w \left[\frac{(1-\alpha)\gamma \left(\frac{\lambda}{1+r} \right)^{\alpha\gamma}}{w} \right]^{\frac{1}{1-(1-\alpha)\gamma}}. \end{aligned}$$

C Optimality Conditions

The first-order conditions for an interior solution to the household's problem are:²⁵

$$\begin{aligned}
 w \left(\bar{l} + \psi h - \psi (1-s) \eta \xi \frac{h}{s} \right) u'(c) &= \\
 \beta \sum_{z', x'} \pi(z', x' | z, x) v_1(\omega', z', x') \omega'_2(q, h, x) \eta \xi \frac{h}{s} \\
 \left(1 - w \psi (1-s) (1-\eta) \xi \frac{h}{e} \right) u'(c) &= \\
 \beta \sum_{z', x'} \pi(z', x' | z, x) v_1(\omega', z', x') \omega'_2(q, h, x) (1-\eta) \xi \frac{h}{e} \\
 \frac{1}{1+r} u'(c) &= \beta \sum_{z', x'} \pi(z', x' | z, x) v_1(\omega', z', x') \omega'_1(q, h, x).
 \end{aligned}$$

D Aggregation

The individual input demands from problem (P^f) can be written as

$$\begin{aligned}
 l &= \frac{a^* \left[\frac{1-\tau_a}{(1+\tau_k)^{\alpha\gamma}} \right]^{\frac{1}{1-\gamma}}}{\int_M a^* \left[\frac{1-\tau_a}{(1+\tau_k)^{\alpha\gamma}} \right]^{\frac{1}{1-\gamma}} d\Psi} L \equiv \varpi_l L \\
 k &= \frac{a^* \left[\frac{1-\tau_a}{(1+\tau_k)^{1-\gamma(1-\alpha)}} \right]^{\frac{1}{1-\gamma}}}{\int_M a^* \left[\frac{1-\tau_a}{(1+\tau_k)^{1-\gamma(1-\alpha)}} \right]^{\frac{1}{1-\gamma}} d\Psi} K \equiv \varpi_k K.
 \end{aligned}$$

²⁵Notice that v_1 is always defined at the optimum. Even though v has a kink in the wealth dimension induced by the occupational choice, the optimum will never occur at this kink. It follows that, at the optimum, v_1 is either equal to v_1^w or to v_1^e . Notice also that, with sufficient smoothness introduced by the ability shocks, which we assume, the first-order conditions are not only necessary but also sufficient for an optimum. See [Clausen and Strub \(2013\)](#) for a formal discussion.

Aggregate production is then

$$\begin{aligned}
Y &= \int_M y d\Psi \\
&= \int_M (1 - \tau_a) (a^*)^{1-\gamma} \left(k^\alpha l^{1-\alpha} \right)^\gamma d\Psi \\
&= TFP \left(K^\alpha L^{1-\alpha} \right)^\gamma
\end{aligned}$$

where

$$TFP \equiv \int_M (1 - \tau_a) (a^*)^{1-\gamma} \varpi_k^{\alpha\gamma} \varpi_l^{(1-\alpha)\gamma} d\Psi.$$

E Mapping Between Model and Data

The aggregate production function in the data is

$$Y = TFP \left(K^\alpha L^{1-\alpha} \right)^\gamma,$$

where $L \equiv h\ell N$ is the total labor input, with h being human capital per worker, ℓ the total number of workers per engaged person, and N the number of engaged persons (which includes workers and the self-employed).

We proceed in a way analogous to the related literature employing decreasing returns to scale technology (e.g. [Buera and Shin, 2013](#)) and abstract from scale effects. That is, we treat the data as if $N = 1$ for both the U.S. and India, and rewrite the aggregate production function in terms of (lowercase) variables per engaged person as

$$y = TFP \left(k^\alpha (h\ell)^{1-\alpha} \right)^\gamma.$$

We rely on PWT8.1 data in order to back out measured TFP for the U.S. and India. We use data for the year 2005 on current-year PPP-adjusted GDP per engaged person (variable $CGDP^o$ divided by EMP), capital stock per engaged person (CK/EMP), and human capital stock per engaged person (variable HC), together with our parameter values for α and γ . The PWT8.1 provide human capital stock estimates by mapping average years of schooling from [Barro and Lee \(1993\)](#) through an exponential human capital technology specification as in [Caselli \(2005\)](#), using returns to schooling specific to each schooling level.

We assume that human capital per worker h , which we do not observe in PWT8.1, equals human capital per engaged person. The total labor input $h\ell$ is then computed by equating ℓ to one minus the rate of entrepreneurship from Table 5.

F Numerical Algorithm

We solve the model using value function iteration.

1. **Discretization:** Discretize ω into $\{\omega_0, \dots, \omega_{N_\omega}\}$. We choose the upper bound and lower bounds such that increasing them further apart has a negligible effect on the solution.

The VAR(1) process for abilities is discretized into a Markov chain using the procedure described in [Tauchen and Hussey \(1991\)](#).

2. **Occupational choice and production:** Solve for $\omega' (q, h, x)$ given the current guess for prices w and r .

(i) Compute the threshold level of saving $q^* (h, x)$.

(ii) Compute profits $\Pi (q, h, x)$.

(iii) Compute next generation's wealth $\omega' (q, h, x)$.

3. **Saving and education:** Solve for the decision rules $e (\omega, z, x)$, $s (\omega, z, x)$, and $q (\omega, z, x)$, given $\omega' (q, h, x)$ from step 2, and given the current guess for prices.

(i) Guess value function $V^j (\omega, z, x)$ at gridpoints.

(ii) Solve for the right-hand-side of the Bellman equation:

$$V^{j+1} (\omega, z, x) = \max_{c, e, s, q} \left\{ u(c) + \beta \sum_{z', x'} \pi(z', x' | z, x) V^j (\omega' (q, h, x), z', x') \right\}$$

subject to (4)-(6).

First try an interior solution for q . If $q \geq -\lambda\phi \max\{\omega, 0\}$ then the solution has been found. Otherwise set $q = -\lambda\phi \max\{\omega, 0\}$ and find s and e subject to this constraint. V^j is approximated by a piecewise linear function for future wealth levels outside of the grid.

(iii) Iterate until $V^j (\omega, z, x) \approx V^{j+1} (\omega, z, x)$.

4. **Invariant distribution:** Approximate by simulating a large cross-section of N agents over a sufficiently large number of T periods. Decision rules are linearly interpolated over a very fine grid. The invariant distribution of individual states $\{\omega_n, z_n, x_n\}_{n=1}^N$ is the period T outcome.

5. **Market clearing:** Check whether the labor and capital markets clear. Compute excess demand for labor and capital from the invariant distribution as:

$$EDL(w, r) = \frac{1}{N} \sum_{n=1}^N [\mathbb{1}_n l_n + s_n \bar{l} - (1 - \mathbb{1}_n) h_n - (1 - s_n) \psi h_n]$$

$$EDK(w, r) = \frac{1}{N} \sum_{n=1}^N \left(\mathbb{1}_n k_n - \frac{q_n}{1+r} \right),$$

where $\mathbb{1}_n$ is an indicator which takes the value of 1 if household n chooses entrepreneurship and 0 otherwise, and the remaining variables indexed by n are the optimal decision rules as a function of the individual state n . Iterate on market prices until $EDL(w, r) \approx 0$ and $EDK(w, r) \approx 0$.